PMT

Ques	stion		Marking details	Marks Available
1	(a)	(i)	Increase (change) in the internal energy [of the system]	1
		(ii)	Heat supplied to (flowing into) [the system]	1
		(iii)	Work done by the system	1
	<i>(b)</i>		PV = nRT	
			$T = \frac{PV}{nR} (1) = \frac{(1.01 \text{ x} 10^5) (1.3 \text{ x} 1.00 \text{ x} 10^{-2})}{(0.4) (8.31)} = 395 \text{ K} (1) \text{ unit mark}$	2
	(c)	(i)	$(1.01 \text{ x}10^5) (0.3 \text{ x} 1.00 \text{ x}10^{-2}) = 303 \text{ [J] on gas } (1)$	
		(ii)	0 / No work (1)	
		(iii)	$\frac{1}{2}(0.3 \times 1.00 \times 10^{-2})(0.2 \times 1.01 \times 10^{5}) + (0.3 \times 1.00 \times 10^{-2})(1.01 \times 10^{5})$	
			= 30 + 303	
			= 333 [J] (1) by gas ecf from (c)(i) (1)	4
	(d)		Convincing evidence of multiplication by 3 for the 3 cycles (1)	
			$\Delta U = 0 \ (1)$	
			$Q = \Delta U + W = 0 + 90 = 90[J]$ into gas (1) ecf from (c)(iii)	3
			Question 1 total	[12]

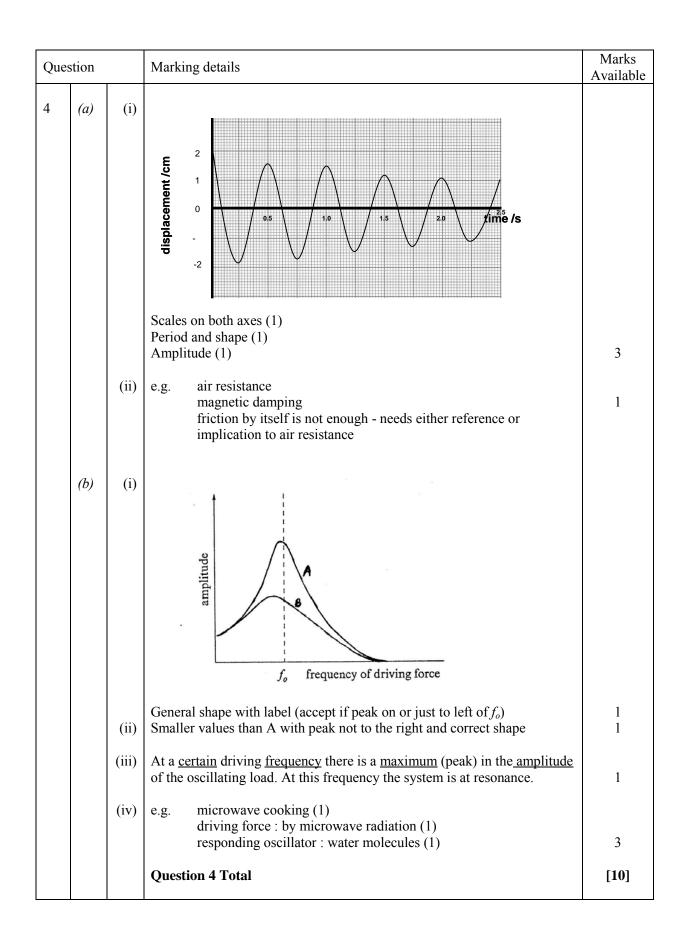
PMT

Question			Marking details	Marks Available
2	(a)	(i)	$Ft = \Delta (mv) \qquad \therefore 3 (0.15) = 0.200 v \qquad v = 2.25 \text{ [m s}^{-1}\text{]}$ Or equivalent but clear method must be shown	1
		(ii)	$(0.200) (2.25) = (0.200 + m_B) (1.20)$ (attempting to use conservation of momentum) (1)	
			$m_{\rm B=} \frac{(0.200)(2.25) - (0.200)(1.20)}{120}$ (1) = 0.175 [kg]	2
		(iii)	KE before collision = $\frac{1}{2}(0.200)(2.25)^2 = 0.506[J](1)$	
			KE after collision = $\frac{1}{2}(0.200)(0.15)^2 + \frac{1}{2}(0.175)(2.40)^2 = 0.506$ [J] (1)	3
			KE before collision = KE after collision [so collision is elastic] (1)	
	<i>(b)</i>	(i)	$E = hf = \frac{hc}{\lambda}(1) = \frac{6.63x10^{-34}x3x10^8}{500x10^{-9}} = 3.98x10^{-19} [J] (1)$	2
		(ii)	N° arriving each second = $\frac{(1500) (100)}{(3.98 \times 10^{-19})} = 3.77 \times 10^{23}$ allow ecf for <i>E</i> from (i)	1
		(iii)	Momentum of 1 photon $= \frac{\hbar}{\lambda} = \frac{(6.63 \times 10^{-34})}{(500 \times 10^{-9})} (1) = 1.33 \times 10^{-27} [\text{kg m s}^{-1}]$ Change of momentum of 1 photon 2 (1) x 1.33 \times 10^{-27} = 2.65 \times 10^{-27} [\text{kg m s}^{-1}]	
			Total change of momentum of photon in 1 s = $(2.65 \times 10^{-27}) (3.77 \times 10^{23}) = 9.99 \times 10^{-4} [\text{kg m s}^{-1}] (1)$	
			Allow ecfs from (b)(i) and (ii)	
			Force = Change of momentum per second = $9.99 \times 10^{-4} = 1.0 \times 10^{-3}$ [N]	2
			(force on sail is equal and opposite to force on photons)	3
			Question 2 total	[12]

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Marks Availabl	e

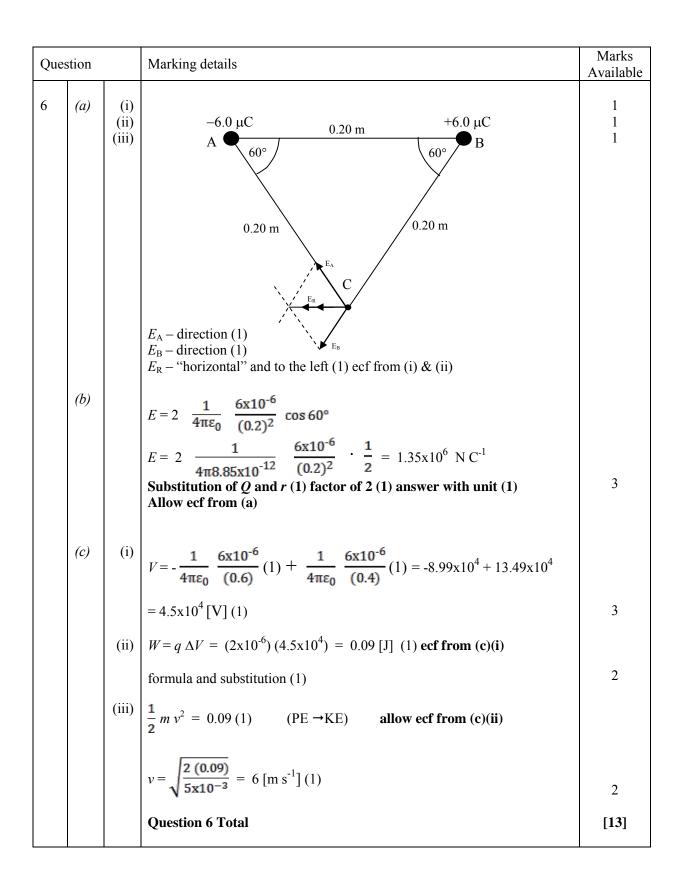
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Que	stion		Marking details	Marks Available
3	(a)		Acceleration $\alpha$ displacement from central (fixed) point (1)	
			is directed towards the central (fixed) point (1)	2
	<i>(b)</i>	(i)	$\omega = \frac{2\pi}{T} = \frac{2\pi}{0.40} = 15.7 [\text{rad s}^{-1}](1)$	2
			$v_{\text{max}} = \omega A = (15.7) (0.05) = 0.79 [\text{m s}^{-1}] (1)$	2
		(ii)	$a_{\text{max}} = \omega^2 A(1) = (15.7)^2 (0.05) = 12.3 \text{ [m s}^{-2}\text{]}(1)$	2
	(c)		$x = 0.05 \sin\left(15.7t - \frac{\pi}{2}\right)$ [m]	
			0.05 (1) 15.7 (1) $-\frac{\pi}{2}$ (1) or accept -90°	3
	(d)		Loses contact when $a = -g(1)$	
			$-\omega^2 x = -g$	
			$x = \frac{9.81}{(15.7)^2} = 0.04  [\text{m}]  (1)$	2
			Question 3 total	[11]



Question			Marking details	Marks Available
5	(a)	(i)	PV = n RT	
			$n = \frac{PV}{RT} = \frac{(3.04 \times 10^5)(0.025)}{(8.31)(280)} = 3.27[\text{mol}]$	1
		(ii)	$N = n N_A = (3.27) (6.02 \times 10^{23}) = 1.97 \times 10^{24}$ allow ecf from (i)	1
		(iii)	$\rho = \frac{\left(mr \times 10^{-3}\right)n}{V} = \frac{\left(4x10^{-3}\right)(3.27)}{0.025} = 0.52[\text{ kg m}^{-3}] (1)$	
			formula with $m_{\rm r}$ (1)	2
		(iv)	$P = \frac{1}{3} \rho \overline{c^2}$	
			$\sqrt{\overline{c^2}} = \sqrt{\frac{3P}{\rho}} = \sqrt{\frac{3(3.04x10^5)}{0.52}} = 1324[ms^{-1}]$ (1) allow ecf from (iii)	2
			Rearrange equation (1)	
	(b)	(i)	(Combining of the two given equations to give) $\frac{1}{3}Nmc^2 = nRT$ (1)	
			KE of gas (i.e. of the <i>N</i> molecules) = $\frac{1}{2} Nm\overline{c^2}$ [ = number of atoms x $\frac{1}{2}m\overline{c^2}$ ] (1) (can award for K.E. of one molecule i.e. K.E. = $\frac{1}{2}m\overline{c^2}$ only if it is	
			clearly noted that it is for one molecule)	
			$\therefore \text{ KE of gas } \left[\frac{1}{2}Nmc^2\right] = \frac{3}{2}nRT \text{ manipulation mark (1)}$ Internal energy of gas (U) = KE + PE and PE = 0 (for ideal gas) (1) [or internal energy is only the KE] (so $U = \frac{3}{2}nRT$ )	4
		(ii)	$U = \frac{3}{2} n RT = \frac{3}{2} (3.27) (8.31) (280) = 11 413 [J]$	1
			Question 5 Total	[11]

PMT



Question		Marking details	Marks Available
7	<i>(a)</i>	<ol> <li>Planets move in elliptical orbits with the Sun at one focus (1)</li> <li>Line joining a planet to the Sun sweeps out equal areas in equal time[ intervals]. (1)</li> <li>r<sup>3</sup> ∝ T<sup>2</sup> r- semi major axis (or accept radius), T- period of orbit (1)</li> </ol>	3
	(b)	Consider $\frac{r^3}{T^2}$ , For Earth $\frac{(149.6 \text{ x}10^9)^3}{(1.00 \text{x}365.25 \text{x}24 \text{x}60 \text{x}60)^2} = 3.36 \text{x}10^{18} \text{ [m}^3 \text{ s}^{-2}](1)$ For Jupiter $\frac{(778.6 \text{ x}10^9)^3}{(11.86 \text{x}365.25 \text{x}24 \text{x}60 \text{x}60)^2} = 3.37 \text{x}10^{18} \text{ [m}^3 \text{ s}^{-2}](1)$	
		Both essentially <b>equal</b> so data consistent with Kepler's third law. (1) (accept answers in other units e.g. $m^3 yr^{-2}$ )	3
	(c)	A body moving in a <u>circular motion</u> experiences an <u>acceleration towards</u> the <u>centre</u> of the circle. This is known as centripetal acceleration.	1
	(d)	$\frac{GM_sm}{r^2} = \frac{mv^2}{r} (1) \qquad \text{m: mass of planet}  \text{or equivalent method}$ $v^2 = \frac{GM_s}{r} \qquad \text{also} \qquad v = \frac{2\pi r}{T} (1)$	
		Combine $\left(\frac{2\pi r}{T}\right)^2 = \frac{GM_s}{r}$ (1) $\frac{4\pi^2 r^2}{T^2} = \frac{GM_s}{r}$	
		$M_s = \frac{4\pi^2}{G}  \frac{r^3}{T^2} = \frac{4\pi^2}{(6.67 \times 10^{-11})}  (3.36 \times 10^{18}) = 2 \times 10^{30}  [\text{kg}] \ (1)$	4
		Question 7 Total	[11]